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## 2017 ACM ICPC Greater New York Regional Contest

## E•Best Rational Approximation

Many microcontrollers have no floating point unit but do have a (reasonably) fast integer divide unit. In these cases it may pay to use rational values to approximate floating point constants. For instance,

$$
355 / 113=3.1415929203539823008849557522124
$$

is a quite good approximation to

$$
\pi=3.14159265358979323846
$$

A best rational approximation, $\boldsymbol{p} / \boldsymbol{q}$, to a real number, $\boldsymbol{x}$, with denominator at most $\boldsymbol{M}$ is a rational number, $\boldsymbol{p} / \boldsymbol{q}$ (in lowest terms), with $\boldsymbol{q}<=\boldsymbol{M}$ such that, for any integers, $\boldsymbol{a}$ and $\boldsymbol{b}$ with $\boldsymbol{b}<=\boldsymbol{M}$, and $\boldsymbol{a}$ and $\boldsymbol{b}$ relatively prime, $\boldsymbol{p} / \boldsymbol{q}$ is at least as close to $\boldsymbol{x}$ as $\boldsymbol{a} / \boldsymbol{b}$ :

$$
|x-p / q| \leq|x-a / b|
$$

Write a program to compute the best rational approximation to a real number, $\boldsymbol{x}$, with denominator at most $M$.

## Input

The first line of input contains a single integer $\boldsymbol{P},(\mathbf{1} \leq \boldsymbol{P} \leq \mathbf{1 0 0 0})$, which is the number of data sets that follow. Each data set should be processed identically and independently.

Each data set consists of a single line of input. It contains the data set number, $\boldsymbol{K}$, followed by the maximum denominator value, $\boldsymbol{M}(\mathbf{1 5} \leq M \leq \mathbf{1 0 0 0 0 0})$, followed by a floating-point value, $\boldsymbol{x},(\mathbf{0} \leq \mathrm{x}<\mathbf{1})$.

## Output

For each data set there is a single line of output. The single output line consists of the data set number, $\boldsymbol{K}$, followed by a single space followed by the numerator, $\boldsymbol{p}$, of the best rational approximation to $\boldsymbol{x}$, followed by a forward slash (/) followed by the denominator, $\boldsymbol{q}$, of the best rational approximation to $\boldsymbol{x}$.

| Sample Input | Sample Output |
| :--- | :--- |
| 3 | $114093 / 99532$ |
| 1 | 100000.141592653589793238 |
| 2 | 255.14159265359793238 |
| 3 | 15.141592653589793238 |

