## **Problem A: Pythagoras's Revenge**

Source file: revenge.{c, cpp, java}
Input file: revenge.in

The famous Pythagorean theorem states that a right triangle, having side lengths A and B and hypotenuse length C, satisfies the formula

 $A^2 + B^2 = C^2$ 

It is also well known that there exist some right triangles in which all three side lengths are integral, such as the classic:



Further examples, both having *A*=12, are the following:



The question of the day is, given a fixed integer value for *A*, how many distinct integers B > A exist such that the hypotenuse length *C* is integral?

**Input:** Each line contains a single integer *A*, such that  $2 \le A < 1048576 = 2^{20}$ . The end of the input is designated by a line containing the value 0.

**Output:** For each value of *A*, output the number of integers B > A such that a right triangle having side lengths *A* and *B* has a hypotenuse with integral length.

Example input:	Example output:
3 12 2 1048574 1048575 0	1 2 0 1 175

A Hint and a Warning: Our hint is that you need not consider any value for *B* that is greater than  $(A^2-1)/2$ , because for any such right triangle, hypotenuse C satisfies B < C < B + 1, and thus cannot have integral length.

Our warning is that for values of  $A \approx 2^{20}$ , there could be solutions with  $B \approx 2^{39}$ , and thus values of  $C^2 > B^2 \approx 2^{78}$ .

You can guarantee yourself 64-bit integer calculations by using the type long long in C++ or long in Java. But neither of those types will allow you to accurately calculate the value of  $C^2$  for such an extreme case. (Which is, after all, what makes this **Pythagoras's** *revenge*!)