

Southeastern European Regional Programming Contest Bucharest, Romania October 15, 2011

Problem D Roots Intervals

Input File: D.IN Output File: standard output

Program Source File: D.C, D.CPP, D.JAVA

Consider the function $f(x) = \tan(\sin(x)) - \sin(\tan(x)) + \cos(x)^5 - 0.5$ defined on the interval [a,b], and $nb \ge 1$ a series of subintervals $[x_i, x_{i+1}]$, i=1, nb, where $x_1=a$ and $x_{nb+1}=b$. Find the number of subintervals that contain "observable" roots of f(x). A root in a subinterval $[x_i, x_{i+1}]$ is "observable" if the existence of that root can be decided without inspecting the behavior of f(x) for $x_i < x < x_{i+1}$, i.e. a subinterval is a black box and you cannot compute inside the interval.

The program input is from a text file. Each data set in the file stands for a particular interval [a,b] of f(x) and specifies the limits a, b (real numbers) and the integer number nb of subintervals. For each data set the program prints the number of subintervals that contain "observable" roots of f(x). Each result is printed on the standard output from the beginning of a line.

White spaces can occur freely in the input. The input data are correct and terminate with an end of file. An input/output sample for the function $f(x) = 1 - x^2$ is in the table bellow.

| Input | Output |
|---------|--------|
| -2 2 2 | 2 |
| 0 100 5 | 1 |
| -1 1 1 | 1 |